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Stefanie Petermichl, Kelly Bickel and Brett D. Wick* (wick@math.gatech.edu), School of Mathematics, Georgia Institute of Technology, 686 Cherry Street, Atlanta, GA 30332-0160. Bounds for the Hilbert Transform with Matrix Muckenhoupt Weights.

Let W denote a matrix A_2 weight. In this talk we will implement the scalar proof for the square function to deduce related results for vector-valued functions on $L^2(\mathbb{R}, \mathbb{C}^d)$. These results are then used to study the boundedness of the Hilbert transform and Haar multipliers on $L^2(\mathbb{R}, \mathbb{C}^d)$. In particular, we prove that:

$$\|Hf\|_{L^{2}(W)} \lesssim [W]_{A_{2}}^{\frac{3}{2}} \log [W]_{A_{2}} \|f\|_{L^{2}(W)} \|T_{\sigma}f\|_{L^{2}(W)} \lesssim [W]_{A_{2}}^{\frac{3}{2}} \log [W]_{A_{2}} \|\sigma\|_{\infty} \|f\|_{L^{2}(W)}$$

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