Torsion in the homology of arithmetic groups has gained a lot of interest from number theorists recently. In this paper, we formulate a conjecture on the topological complexity of cycles on an arithmetic hyperbolic 3-manifold which implies a certain asymptotic growth for the size of the torsion. We prove our conjecture in two very often occurring cases, using heavy number theoretic machinery. (Received January 13, 2014)