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Matthias Beck* (mattbeck@sfsu.edu), **Ana Berrizbeitia**, **Michael Dairyko**, **Claudia Rodriguez**, **Amanda Ruiz** and **Schuyler Veeneman**. *Parking functions, Shi arrangements, and mixed graphs*.

The *Shi arrangement* is the set of all hyperplanes in \mathbf{R}^n of the form $x_j - x_k = 0$ or 1 for $1 \leq j < k \leq n$. Shi observed in 1986 that the number of regions (i.e., connected components of the complement) of this arrangement is $(n + 1)^{n-1}$. An unrelated combinatorial concept is that of a *parking function*, i.e., a sequence (x_1, x_2, \dots, x_n) of positive integers that, when rearranged from smallest to largest, satisfies $x_k \leq k$. (There is an illustrative reason for the term *parking function*.) It turns out that the number of parking functions of length n also equals $(n + 1)^{n-1}$, a result due to Konheim and Weiss from 1966. A natural problem consists of finding a bijection between the n -dimensional Shi arrangement and the parking functions of length n . Pak and Stanley (1996) and Athanasiadis and Linusson (1999) gave such (quite different) bijections. We will shed new light on the former bijection by taking a scenic route through certain mixed graphs. (Received February 04, 2015)