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**Z. Füredi, A. Kostochka\*** (kostochk@math.uiuc.edu) and **J. Verstraëte**. *Stability in the Erdős–Gallai Theorem on cycles and paths*. Preliminary report.

The Erdős–Gallai Theorem states that for  $k \geq 2$ , every graph of average degree more than  $k - 2$  contains a  $k$ -vertex path. This result is a consequence of a stronger result of Kopylov: if  $t \geq 2$ ,  $k \in \{2t + 1, 2t + 2\}$ ,  $n \geq \frac{5t-3}{2}$ , and  $G$  is an  $n$ -vertex 2-connected graph with at least  $h(n, k, t) = \binom{k-t}{2} + t(n - k + t)$  edges, then  $G$  contains a cycle of length at least  $k$  unless  $G = H_{n,k,t} := K_n - E(K_{n-t})$ . We prove a stability version of the Erdős–Gallai Theorem: For all  $n \geq 3t > 3$ , and  $k \in \{2t + 1, 2t + 2\}$ , every  $n$ -vertex 2-connected graph  $G$  with  $e(G) > h(n, k, t - 1)$  either contains a cycle of length at least  $k$  or contains a set of  $t$  vertices whose removal gives a star forest. In particular, if  $k = 2t + 1 \neq 7$ , then  $G \subseteq H_{n,k,t}$ . The lower bound  $e(G) > h(n, k, t - 1)$  in these results is tight. (Received August 03, 2015)