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**Tathagaata Basak\*** ([tathagat@iastate.edu](mailto:tathagat@iastate.edu)), 450 Carver Hall, Iowa State University, Ames, IA 50011. *Modular lattices from finite projective planes.*

Let  $q$  be a prime power. Using geometry of the finite projective plane  $\mathbb{P}^2(\mathbb{F}_q)$  we construct a Hermitian Lorentzian lattice  $L_q$  of dimension  $(q^2 + q + 2)$  defined over a certain number ring that depends on  $q$ . We show that infinitely many of these lattices are modular, that is, the dual lattice of  $L_q$  is isometric to a scaled copy of  $L_q$ . Under certain conditions on  $q$ , the Lorentzian lattice  $L_q$  yields an even self dual positive definite  $2q(q + 1)$  dimensional  $\mathbb{Z}$ -lattice  $M_q$  whose automorphism group contains the automorphisms of  $\mathbb{P}^2(\mathbb{F}_q)$ . General conjectures about prime numbers imply that there are infinitely many such prime numbers  $q = 3, 47, 59, 71, 131 \dots$ . We find that  $M_3$  is the Leech lattice and automorphism group of the Lorentzian lattice  $L_3$  seems to be closely related to the monster simple group. (Received August 05, 2015)