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Joel Clarke Gibbons* (jgibbons@chicagobooth.edu), P.O. Box 63, Saint Joseph, MI 49085,
and **Yusheng Luo** (yusheng@nus.edu). *Colorings of the n -sphere and Inversive Geometry.*

This paper shows that in dimensions $n \geq 2$, for any partition of the set of points in the standard unit n -sphere P_n in $\mathbb{R}^{(n+1)}$ into $(n + 3)$ or more nonempty sets, there exists a hyperplane in $\mathbb{R}^{(n+1)}$ that intersects at least $(n+2)$ of these sets. This result is used to prove a result in inversive geometry. A mapping $T : S^2 \rightarrow S^n$, for $n \geq 2$, not assumed continuous or even measurable, is called weakly circle-preserving if the image of any circle is contained in some circle in the range space S^n . If such a map T has a range $T(S^2)$ in circular general position, meaning that any circle in S^n misses at least two points of $T(S^2)$, then T must be a Möbius transformation of S^2 . (Received March 24, 2015)