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*Pyramids in 3-space and Crystallographic Groups in 4-space.*

The monodromy group  $M(\mathcal{P})$  for a polyhedron  $\mathcal{P}$  (or indeed for any convex, even abstract,  $d$ -polytope  $\mathcal{P}$ ) is a combinatorial invariant of  $\mathcal{P}$ . This group somehow encodes the essential structural features of the polytope. Intuitively,  $M(\mathcal{P})$  describes how an abstract set  $\mathcal{F}$  of *flags* can be assembled to produce  $\mathcal{P}$ .

Recently (*Discrete Mathematics*, in press) we have completely described  $M(\mathcal{P})$  when  $\mathcal{P}$  is an ordinary pyramid over an  $n$ -gonal base. Though  $\mathcal{P}$  itself is very familiar,  $M(\mathcal{P})$  has some interesting features.

Here we focus on the extreme cases  $n = 2$  and  $\infty$ . In the first instance, when  $\mathcal{P}$  is the rather modest pyramid over the digon,  $M(\mathcal{P})$  is, surprisingly, isomorphic to the symmetry group of a 4-cube. And, at the other extreme, when  $n = \infty$ ,  $M(\mathcal{P})$  acts, in a natural way, as a crystallographic group in real 4-space.

But why dimension 4? Well, look at a pyramid and count flag orbits under the action of the automorphism group of the base. (Received January 10, 2014)