We state some old and new results and conjectures on $L^\infty$ bounds of holomorphic sections of powers of a positive line bundle on a compact Kähler manifold.

In particular, we show the existence of sequences of orthonormal bases of sections of all powers of a positive holomorphic line bundle that contain a uniformly bounded subsequence of positive density. (Received January 27, 2014)