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Paul N Balister* (pbalistr@memphis.edu), Department of Math Sciences, University of Memphis, Memphis, TN 38152, and **Bela Bollobas** and **Paul Smith**. *The speed of bootstrap percolation in two dimensions.*

Let \mathbb{T}_n be the n by n discrete torus and assume each vertex of \mathbb{T}_n is initially *infected* with probability p . At each time step, every vertex with at least two infected neighbors becomes infected. It was proved by Holroyd that there is a threshold of $(1 + o(1))\pi^2/18 \log n$ above which the entire torus becomes infected with high probability, and below which the entire torus becomes infected only with very low probability. For p greater than this threshold, we consider the number of steps T_n needed for full infection and show that

$$T_n = \begin{cases} \frac{\log n}{2 \log(1/(1-p))} + O\left(e^{\frac{\pi^2 + o(1)}{9p}}\right) & \text{for } p \gg \frac{1}{\log \log n}; \\ \Theta\left(\sqrt{\frac{\log n}{p}} e^{\frac{\pi^2 + o(1)}{18p}}\right) & \text{for } p \ll \frac{1}{\log \log n}. \end{cases}$$

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