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**Cao Tien Dat** and **Igor Verbitsky\***, Department of Mathematics, University of Missouri, Columbia, MO 65211. *Quasilinear elliptic equations with singular gradient terms of natural growth.*

We give necessary and sufficient conditions for the existence of solutions to quasilinear elliptic equations with singular natural growth in the gradient terms of the type  $-\Delta_p v = b \frac{|\nabla v|^p}{v} + \sigma$  on  $\mathbf{R}^n$ , where  $v > 0$ ,  $b > 0$ , and  $\sigma \geq 0$  is an arbitrary locally integrable function, or measure, and  $\Delta_p u = \operatorname{div}(\nabla u |\nabla u|^{p-2})$  is the  $p$ -Laplacian,  $p > 1$ . Sharp global pointwise estimates and regularity properties of solutions are obtained. The results are new even in the classical case  $p = 2$ . This is joint work with Cao Tien Dat. (Received January 30, 2015)