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Computing power of the ordered field of real numbers. Preliminary report.

The third author defined a reducibility that lets us compare the computing power of uncountable structures. We have $\mathcal{A} \leq_w^* \mathcal{B}$ if in a generic extension of V in which both \mathcal{A} and \mathcal{B} countable, every copy of \mathcal{B} computes a copy of \mathcal{A} . Using this reducibility, we compare the reals with some related structures. Let \mathcal{R} be the ordered field of real numbers. Let \mathcal{R}^* be an ω -saturated extension of \mathcal{R} , and let \mathcal{R}_{exp} be the expansion of \mathcal{R} by the exponential function. The first two authors showed that \mathcal{R} lies strictly above \mathcal{R}^* under \leq_w^* . The extra computing power of \mathcal{R} comes from the fact that it is Archimedean. The structures \mathcal{R} and \mathcal{R}_{exp} turn out to be equivalent. Some other expansions of \mathcal{R} also turn out also not to have added computing power. (Received January 14, 2015)