

1107-11-148

William Kang* (williamkang531@gmail.com). *Efficient Covering Systems of Congruences and Perfect Powers Riesel Numbers*. Preliminary report.

A *Sierpiński* number is an odd integer k such that $k \cdot 2^n + 1$ is composite for all positive integer values of n . A *Riesel* number is defined similarly; the only difference is that $k \cdot 2^n - 1$ is composite for all positive integer values of n .

It is easy to construct Sierpiński (Riesel) numbers k such that k^q is also Sierpiński (Riesel) for every positive odd integer q . Chen asked whether this remains true for even values of q . Recently, Filaseta et al. solved the problem for the Sierpiński case in the affirmative. They also constructed odd numbers k, l, m such that k^2, l^4 , and m^6 , respectively, are Riesel numbers.

In 2009, Wu and Sun showed the existence of an odd k such that k^q is a Riesel number for all positive integers q such that $\gcd(q, 3 \cdot 5 \cdot 7 \cdot 11 \cdot 13) = 1$. In particular, k^{2^s} is Riesel for all $s \geq 0$. In this paper we improve these results as follows:

We construct Riesel numbers k^2, l^4 , and m^6 much smaller than those found by Filaseta, Finch, and Kozek.

We show the existence of an odd positive integer k such that k^q is a Riesel number for all positive integers q such that $\gcd(q, 3 \cdot 5 \cdot 7 \cdot 11) = 1$. This improves Wu and Sun's construction. (Received January 11, 2015)