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The asymptotic patterns of the Betti sequences of the finitely generated modules over a local ring  $R$  reflect and affect the singularity of  $R$ . For instance, these sequences are eventually zero if and only if  $R$  is regular (Auslander and Buchsbaum, Serre) and they are eventually constant if and only if  $R$  is a hypersurface (Shamash, Gulliksen, Eisenbud). We describe those rings over which the next simplest pattern occurs—each Betti sequences is eventually arithmetic. More generally, when  $c$  is a non-negative integer we obtain sufficient conditions and necessary conditions for each Betti sequences to be eventually given by some polynomial of degree less than  $c$ . These conditions coincide when  $c \leq 3$  or when  $R$  is homogeneous. (Received January 14, 2015)