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A *dominating path* in a graph is a path P such that every vertex outside P has a neighbor on P . A result of Broersma from 1988 implies that if G is an n -vertex k -connected graph and $\delta(G) \geq \frac{n-k}{k+2}$, then G contains a dominating path. The lengths of dominating path include all values from the shortest up to at least $\min \{n-1, 2\delta(G)\}$. For $\delta G > an$, where a is a constant greater than $1/3$, the minimum length of a dominating path is at most logarithmic in n when n is sufficiently large (the base of the logarithm depends upon a). The preceding results are sharp. For constant s and $c' < 1$ an s -vertex dominating path is guaranteed by $\delta(G) \geq n-1-c'n^{1-1/s}$ when n is sufficiently large, but $\delta(G) \geq n-c(s \ln n)^{1/s}n^{1-1/s}$ (where $c > 1$) does not even guarantee a dominating set of size s . We obtain minimum degree conditions for the existence of a spanning tree obtained from a dominating path by giving the same number of leaf neighbors to each vertex. (Received August 18, 2015)