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Csaba Biró, Peter Hamburger, H. A. Kierstead, Attila Pór, William T. Trotter*

(trotter@math.gatech.edu) and **Ruidong Wang**. *An Application of the Lovász Local Lemma to Stability Analysis of Dimension*. Preliminary report.

Let $f(c)$ denote the least integer so that if P is a poset with $|P| = 2n + 1$ and $\dim(P) \geq n - c$, then P contains a standard example of dimension $d = n - f(c)$, provided of course that n is sufficiently large. In earlier work, Biró, Hamburger, Pór and Trotter showed that $f(c)$ exists and satisfies $f(c) = O(c^2)$. From below, they used finite projective planes to show that $f(c)$ must be at least as large as $c^{4/3}$. As part of a comprehensive revisit to the subject of the dimension of random posets of height 2 first investigated by Erdős, Kierstead and Trotter more than 20 years ago, we extract an application of the celebrated Lovász Local Lemma to show that $f(c)$ must be at least $c^{3/2}$, ignoring multiplicative terms involving $\log c$. (Received August 24, 2015)