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Recently, the authors improved the bound on the largest gaps between consecutive prime numbers. An important ingredient in the proof is a new result on efficient covering of hypergraphs, which extends a well-known theorem of Pippenger and Spencer from 1989. The Pippenger-Spencer theorem ensures the existence of a near-perfect packing of a hypergraph $H = (V, E)$ under three basic assumptions on H : (a) uniformity - all hyperedges $e \in E$ have the same (bounded) cardinality k ; (b) regularity - the degree of each vertex $v \in V$ is asymptotically the same; (c) small codegrees - for all distinct $v, w \in V$, there are "few" edges containing both v and w . Our new theorem gives essentially the same conclusion (not necessarily a packing, but an efficient near-covering) with a substantial weakening of hypotheses (a) and (b), while retaining (c) and the main hypothesis. (Received July 09, 2015)