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**Z. Füredi, A. Kostochka\*** (kostochk@math.uiuc.edu) and **J. Verstraëte**. *Stability results on cycles and paths*. Preliminary report.

The classical Erdős-Gallai theorems from 1959 on the most edges in  $n$ -vertex graphs not containing paths or cycles with  $k$  edges were sharpened later by Faudree and Schelp, Woodall, and Kopylov. For  $n \geq 5k/4$  the strongest result was: if  $t \geq 2$ ,  $k = 2t + 1$ ,  $n \geq \frac{5t-3}{2}$ , and  $G$  is an  $n$ -vertex 2-connected graph with at least  $h(n, k, t) = \binom{k-t}{2} + t(n - k + t)$  edges, then  $G$  contains a cycle of length at least  $k$  unless  $G = H_{n,k,t} := K_n - E(K_{n-t})$ . We prove stability versions of these results. In particular, if  $n \geq 3t > 3$ ,  $k = 2t + 1$  and the number of edges in an  $n$ -vertex 2-connected graph  $G$  with no cycle of length at least  $k$  is greater than  $h(n, k, t - 1) = \binom{k-t+1}{2} + (t - 1)(n - k + t - 1)$ , then  $G$  is a subgraph of  $H_{n,k,t}$ . The lower bound on  $e(G)$  is tight. (Received August 13, 2015)