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**Ben Wallis\*** (z1019463@students.niu.edu), Dekalb, IL 60115, and **Gleb Sirotkin**. *Closed ideals in  $\mathcal{L}(X)$  and  $\mathcal{L}(X^*)$  when  $X$  contains certain copies of  $\ell_p$  and  $c_0$ .*

Let  $X$  denote a Banach space, and let  $\mathcal{L}(X)$  denote the space of continuous linear operators acting on  $X$ . An ideal of  $\mathcal{L}(X)$  is a linear subspace  $\mathcal{J}$  of  $\mathcal{L}(X)$  which is closed under composition with arbitrary operators in  $\mathcal{L}(X)$ , i.e. such that if  $A, B \in \mathcal{L}(X)$  and  $T \in \mathcal{J}$  then  $BTA \in \mathcal{J}$ . It is called closed if it is closed in the norm topology of  $\mathcal{L}(X)$ . We show that there are uncountably many closed ideals in  $\mathcal{L}(\ell_p \oplus \ell_q)$  for  $1 \leq p < q \leq \infty$ , and in  $\mathcal{L}(\ell_p \oplus c_0)$  for  $1 \leq p < 2$ . This finishes answering a longstanding question of Pietsch (1978). Additional results are obtained for Rosenthal's  $X_p$  spaces and Woo's  $X_{p,r}$  generalizations thereof. This is joint work with Gleb Sirotkin. (Received August 24, 2015)