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Inspired by ideas of Schatten in his celebrated monograph [*A theory of cross-spaces*, 1950], we introduce the notion of a Lipschitz tensor product $X \boxtimes E$ of a pointed metric space X and a Banach space E as a certain linear subspace of the algebraic dual of $\text{Lip}_0(X, E^*)$, where $\text{Lip}_0(X, E^*)$ denotes the space of Lipschitz functions from X to E^* .

We show that the Lipschitz injective norm ε , the Lipschitz projective norm π and the Lipschitz p -nuclear norm d_p ($1 \leq p \leq \infty$) are uniform dualizable Lipschitz cross-norms on $X \boxtimes E$ and study their properties.

On the other hand, for a Lipschitz cross-norm α on $X \boxtimes E$, we introduce the notion of α -Lipschitz operators from X into E^* and prove that the space $\text{Lip}_\alpha(X, E^*)$ of such Lipschitz operators under the α -Lipschitz norm Lip_α is isometrically isomorphic to the dual space of $X \boxtimes_\alpha E$.

In addition, if p' denotes the conjugate index of p , we show that $\text{Lip}_{d_p}(X, E^*)$ is justly the space of all Lipschitz p' -summing operators from X to E^* (introduced by Farmer and Johnson) and therefore such space can be identified with $(X \boxtimes_{d_p} E)^*$. (Received August 17, 2015)