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Thin sequences, model spaces, and Douglas algebras.

Let (z_n) be a sequence in the open unit disk and T_p an operator taking an H^p function f to the sequence $(f(z_n)(1-|z_n|)^{1/p})$. Shapiro and Shields found conditions for the sequence to be interpolating; e.g, the range $T_p(H^p)$ equals the sequence space ℓ^p and the condition is Carleson's condition:

$$\inf_k \prod_{n \neq k} \left| \frac{z_k - z_n}{1 - \bar{z}_n z_k} \right| \geq \delta > 0.$$

We consider interpolating sequences for model spaces, $K_\theta := H^2 \ominus \theta H^2$, associated with an inner function θ . If we have a sequence for which the restriction of T_2 maps K_θ onto ℓ^2 , then T_2 will map H^2 onto ℓ^2 . For which sequences can we be sure that if $T_2 : H^2 \rightarrow \ell^2$ is surjective, then the restriction $T_2 : K_\theta \rightarrow \ell^2$ is surjective?

We answer this for the class of *thin sequences* – interpolating sequences for which $\lim_{k \rightarrow \infty} \prod_{j; j \neq k} \left| \frac{z_j - z_k}{1 - \bar{z}_j z_k} \right| = 1$. The answer depends on the sequence and the inner function. We also consider the same question for H^∞ and subalgebras of L^∞ that properly contain H^∞ . (Received July 29, 2015)