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**Mark Reeder\*** (reederma@bc.edu). *Dyadic Exercises in Exceptional Groups*. Preliminary report.

Let  $\Gamma$  be the absolute Galois group of the field  $\mathbb{Q}_2$  of dyadic numbers and let  $\mathfrak{g}$  be a simple complex Lie algebra of rank  $r$ . We study the Swan conductors  $sw(\varphi, \mathfrak{g})$  of continuous representations  $\varphi : \Gamma \rightarrow G$ , where  $G$  is the group of inner automorphisms of  $\mathfrak{g}$ .

**Conjecture:** *Assume that  $\varphi$  is totally ramified. Then  $sw(\varphi, \mathfrak{g}) \geq r$  and if  $sw(\varphi, \mathfrak{g}) = r$  then  $\varphi$  is unique up to conjugacy in  $G$ .*

There is a variant of this conjecture for more general representations  $\varphi : \Gamma \rightarrow \text{Aut}(\mathfrak{g})$ . The conjecture is known for  $\mathfrak{g}$  of type  $A_n$  and  $G_2$ . In general it is implied by the Local Langlands Conjecture.

Let  $\mathfrak{h} < \mathfrak{k} < \mathfrak{g}$  be the natural chain of Lie algebras of type  $D_4, F_4$  and  $E_6$ . We verify the inequality in the conjecture for  $\mathfrak{k}, \mathfrak{g}$  and its variant for the triality group  $H \cdot 3 < \text{Aut}(\mathfrak{h})$ , and we describe a solvable filtered subgroup  $D < H \cdot 3$  of order  $64 \cdot 21 \cdot 64 \cdot 8 \cdot 4$  such that if the Swan conductor of  $\varphi$  attains its lower bound in any of the three cases then the image of  $\varphi$  is conjugate to  $D$ . (Received September 20, 2015)