Given a function field $K$ of characteristic 0 and a prime (or a valuation) of this field, we discuss how to construct an existential definition of the subring of $K$ containing functions without a pole at the given prime. This problem was solved for a class of rational function fields in 1992 by Kim and Roush but was not completely generalized to algebraic extensions until now. (Received January 10, 2017)