

1126-11-393

**Kirsten Eisentraeger** (eisentra@math.psu.edu), State College, PA 16802, **Russell Miller** (russell.miller@qc.cuny.edu), New York, NY 11367, **Jennifer Park\*** (jmypark@umich.edu), Ann Arbor, MI 48109, and **Alexandra Shlapentokh** (shlapentokha@ecu.edu), Greenville, NC 27858. *Hilbert's tenth problem for subrings of  $\mathbb{Q}$ .*

Determining whether there is an algorithm that decides the  $\mathbb{Q}$ -solvability of polynomials with integer coefficients is a very difficult open problem, although we know that there are no algorithms that decides the  $\mathbb{Z}$ -solvability of polynomials by the work of Matiyasevich, Davis, Putnam, and Robinson. In this talk, we construct a ring  $R$  that is "close" to  $\mathbb{Z}$ : namely, a ring of the form  $\mathbb{Z}[S^{-1}]$ , where  $S$  is a "small" set of primes that are inverted in  $R$ . Then we will show that determining the  $R$ -solvability of polynomials is just as hard as determining the  $\mathbb{Q}$ -solvability of polynomials, using the notion of Turing equivalence. This work is joint with K. Eisentraeger, R. Miller, and A. Shlapentokh. (Received January 17, 2017)