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Jozsef Balogh*, University of Illinois at Urbana Champaign, Urbana, IL, and **Shagnik Das**,
Michelle Delcourt, **Hong Liu** and **Maryam Sharifzadeh**. *Intersecting families of discrete
structures are typically trivial.*

The study of intersecting structures is central to extremal combinatorics. A family of permutations $F \subset S_n$ is *t-intersecting* if any two permutations in F agree on some t indices, and is *trivial* if all permutations in F agree on the same t indices. A k -uniform hypergraph is *t-intersecting* if any two of its edges have t vertices in common, and *trivial* if all its edges share the same t vertices. The fundamental problem is to determine how large an intersecting family can be. Ellis, Friedgut and Pilpel proved that for n sufficiently large with respect to t , the largest t -intersecting families in S_n are the trivial ones. The classic Erdős–Ko–Rado theorem shows that the largest t -intersecting k -uniform hypergraphs are also trivial when n is large. We determine the *typical* structure of t -intersecting families, extending these results to show that almost all intersecting families are trivial. We also obtain sparse analogues of these extremal results, showing that they hold in random settings. Our proofs use the Bollobás set-pairs inequality to bound the number of maximal intersecting families, which can then be combined with known stability theorems. (Received January 18, 2015)