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Yang Wang*, Department of Mathematics, Hong Kong University of Science and Technology,
Kowloon, Hong Kong. *Self-Similar Subsets of the Cantor Set.*

We study the following question proposed by Mattila in 1998: what are the self-similar subsets of the middle-third Cantor set C ? For any non-trivial self-similar subset F of C , we show that any linear generating IFS of F should consist of similitudes whose contraction ratios are integer powers of $1/3$. Furthermore, we provide necessary and sufficient conditions to characterize all self-similar subsets of C . A very simple criterion is formulated to characterize self-similar subsets of C with equal contraction ratio. For the general case a finite algorithm is provided to generate all self-similar subsets of C with pre-given contraction ratios. (Received January 20, 2015)