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Yuval Peres*, 1 Microsoft Way, Redmond, WA 98052. *Monotone restrictions of Brownian motion, variable drift and self-affine graphs.*

I will present two recent fractal studies of Brownian graphs. Let $\{B(t): 0 \leq t \leq 1\}$ be a linear Brownian motion and let $\alpha > \frac{1}{2}$. In joint work with Richard Balka (University of Washington), we prove that, almost surely, there is no set $A \subset [0, 1]$ such that its Hausdorff dimension $\dim A > \frac{1}{2}$ and $B: A \rightarrow \mathbb{R}$ is α -Hölder continuous. The proof uses Kaufman's dimension doubling theorem for planar (!) Brownian motion. We deduce that, almost surely, there is no set $A \subset [0, 1]$ such that $\dim A > \frac{1}{2}$ and $B: A \rightarrow \mathbb{R}$ is weakly increasing. The second topic is joint work with Perla Sousi (Cambridge). For any Borel function f from the unit interval to \mathbf{R}^d , we express the Hausdorff dimension of the image and the graph of $B + f$ in terms of f . When the graph of f is a self-affine McMullen-Bedford carpet, we obtain an explicit formula for the dimension of the graph of $B + f$ in terms of the generating pattern. In particular, we show that it can be strictly bigger than the maximum of the Hausdorff dimensions of the graphs of f and B . Despite the random perturbation, the Minkowski and Hausdorff dimensions of the graph of $B + f$ can disagree. (Received January 17, 2015)