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**Patricia Jacobs Klein\*** (triciaj@umich.edu). *Asymptotic behavior of certain Koszul cohomology modules.*

Let  $(R, m)$  be a local ring,  $M$  a finitely generated module over  $R$ , and  $f_1, \dots, f_d$  a system of parameters on  $M$ . Lech's limit formula states that as  $\min_i t_i \rightarrow \infty$

$$\frac{\ell(M/(f_1^{t_1}, \dots, f_d^{t_d})M)}{t_1 \cdots t_d} \longrightarrow e(f_1, \dots, f_d \mid M),$$

the multiplicity of  $(f_1, \dots, f_d)$  on  $M$ . One may ask whether powers of a fixed sequence of parameters may be replaced by any sequence of parameter ideals  $I_n$  such that  $I_n \subseteq m^n$ . Recalling that the multiplicity may be realized as the alternating sum of the lengths of Koszul cohomology modules and that  $H^n(f_1^{t_1}, \dots, f_d^{t_d} \mid M) \cong M/(f_1^{t_1}, \dots, f_d^{t_d})M$ , we rewrite Lech's limit formula as follows

$$\frac{\sum_{j=0}^n (-1)^{n-j} \ell(H^j(f_1^{t_1}, \dots, f_d^{t_d}; M))}{\ell(H^n(f_1^{t_1}, \dots, f_d^{t_d}))} \longrightarrow 1.$$

From this point of view, it is also natural to ask in the case when  $\dim M = \dim R = d$  for which  $i < d$  we have  $\ell(H^i(I_n; M))/\ell(R/I_n R) \rightarrow 0$ . The main result is that when  $M$  is faithful, the  $M$  satisfying the condition that  $\ell(H^i(I_n; M))/\ell(R/I_n R) \rightarrow 0$  for all  $i < d$  and all parameter  $I_n \subseteq m^n$  are exactly those  $M$  that are locally Cohen-Macaulay. (Received February 26, 2017)