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**Jillian Louise Glassett\*** (jglassett@math.wsu.edu), jglassett@math.wsu.edu, and **Judith McDonald.** *Spectrally Arbitrary Zero-Nonzero Patterns over Rings with Unity.*

A zero-nonzero matrix pattern  $\mathcal{A}$  is a square matrix with entries  $\{0, *\}$ . A  $n \times n$  pattern  $\mathcal{A}$  is spectrally arbitrary over a ring  $\mathcal{R}$  if for each  $n$ -th degree monic polynomial  $f(x) \in \mathcal{R}[x]$ , there exist a matrix  $A$  over  $\mathcal{R}$  with pattern  $\mathcal{A}$  such that the characteristic polynomial  $p_A(x) = f(x)$ . A  $n \times n$  pattern  $\mathcal{A}$  is relaxed spectrally arbitrary over  $\mathcal{R}$  if for each  $n$ -th degree monic polynomial  $f(x) \in \mathcal{R}[x]$ , there exist a matrix  $A$  over  $\mathcal{R}$  with either pattern  $\mathcal{A}$  or a subpattern of  $\mathcal{A}$  such that the characteristic polynomial  $p_A(x) = f(x)$ . We consider whether a pattern  $\mathcal{A}$  that is spectrally arbitrary over a ring  $\mathcal{R}$  is spectrally arbitrary or relaxed spectrally arbitrary over another ring  $\mathcal{S}$ . In particular, we discovered that a pattern that is spectrally arbitrary over  $\mathbb{Z}$  is relaxed spectrally arbitrary over  $\mathbb{Z}_m$  for all  $m$ . We also determined the minimum number of  $*$  entries to be spectrally arbitrary over  $\mathbb{Z}$ . (Received February 22, 2017)