

1128-35-249

Hart F Smith* (hfsmith@uw.edu), University of Washington, Box 354350, Seattle, WA 98195-4350. *On the trace of Schrödinger heat kernels and regularity of potentials.*

We consider the Schrödinger operator $-\Delta_g + V$ on a complete Riemannian manifold (M, g) , with a bounded real potential V of compact support, and establish a sharp equivalence between Sobolev regularity of V and the existence of finite-order asymptotic expansions as $t \rightarrow 0$ of the relative trace of the Schrödinger heat kernel. Precisely, under the hypothesis $V \in L_{\text{comp}}^\infty(M)$ is real valued, then $V \in H^m(M)$ if and only if there are constants c_j so that

$$\text{tr}(e^{-tP_V} - e^{-tP_0}) = (4\pi t)^{-\frac{n}{2}} \left(c_1 t + c_2 t^2 + \cdots + c_{m+1} t^{m+1} + \mathcal{O}(t^{m+2}) \right).$$

As an application, we generalize a result of Sà Barreto and Zworski on the existence of resonances on compact metric perturbations of three-dimensional Euclidean space, to the case of bounded measurable potentials. (Received February 27, 2017)