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Let  $\{\varphi_i\}_{i=0}^{\infty}$  be a sequence of orthonormal polynomials on the unit circle with respect to a probability measure  $\mu$ . We study zero distribution of random linear combinations of the form

$$P_n(z) = \sum_{i=0}^{n-1} \eta_i \varphi_i(z),$$

where  $\eta_0, \dots, \eta_{n-1}$  are i.i.d. standard Gaussian variables. We use the Christoffel-Darboux formula to simplify the density functions provided by Vanderbei for the expected number real and complex of zeros of  $P_n$ . From these expressions, under the assumption that  $\mu$  is in the Nevai class, we deduce the limiting value of these density functions away from the unit circle. Under the mere assumption that  $\mu$  is doubling on subarcs of the unit circle centered at 1 and  $-1$ , we show that the expected number of real zeros of  $P_n$  is at most

$$(2/\pi) \log n + O(1),$$

and that equality holds when  $\mu$  is in the Szegő-Bernstein class. We conclude with providing discrepancy results that estimate the expected number of complex zeros of  $P_n$  in shrinking neighborhoods of compact subsets of the unit circle. (Received January 25, 2017)