

1121-05-134

**Aba Mbirika\*** (mbirika@uwec.edu), University of Wisconsin-Eau Claire, and **Julianna Tymoczko**. *Combinatorial questions related to the representation stability of the cohomology of Springer varieties*. Preliminary report.

The Springer variety  $\mathfrak{S}_X$  is the set of flags stabilized by a nilpotent operator  $X \in \text{Mat}_n(\mathbb{C})$ . Each nilpotent operator corresponds to a partition  $\mu_n$  of  $n$  via decomposition of  $X$  into Jordan canonical blocks. The Springer representation arises when the symmetric group  $S_n$  acts on the cohomology ring of this family of varieties. Constructed by Springer in 1976, this ring  $H^*(\mathfrak{S}_X)$  was later given a simplified presentation by Concini and Procesi, then refined by Tanisaki who simplified the Concini-Procesi ideals, and finally Garsia and Procesi who gave a basis for  $H^*(\mathfrak{S}_X)$  as a quotient  $R(n)/I_{\mu_n}$  where  $R(n) = \mathbb{C}[x_1, \dots, x_n]$  and the  $I_{\mu_n}$  are the Tanisaki ideals.

We present some combinatorial aspects that arise in the representation stability of the sequence  $\{H^*(R(n)/I_{\mu_n})\}_{n=1}^{\infty}$ . In joint work with Tymoczko, we describe the co-FI-module structure (in the sense of Church, Ellenberg, and Farb) of this sequence. A surprising feature of the proof is that this structure exists for every possible sequence  $\mu_1 \subseteq \mu_2 \subseteq \dots$  of Young diagrams. We explore some combinatorial questions related to this representation stability of the Springer representation. (Received July 16, 2016)