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We investigate the ways in which fundamental properties of the weak Bruhat order on a Weyl group can be lifted (or not) to a corresponding highest weight crystal graph, viewed as a partially ordered set. The latter projects to the weak order via the so-called key (poset) map, defined based on the Demazure crystal structure. We work mostly in symmetrizable Kac-Moody generality, and first give positive results for lower intervals in a crystal poset. The main ones are: the analogue of the word property, the fact that the Möbius function is always 0 or ± 1 , and that the corresponding order complexes are homotopy equivalent to balls or spheres. Then we show that these results fail for arbitrary intervals, even in type A. (Received August 21, 2016)