

1123-05-171

**Jacques Verstraete\*** (jacques@ucsd.edu), 9500 Gilman Drive, La Jolla, CA 92093-0112, and  
**Michael Molloy** and **Benjamin Sudakov**. *On Relative Turán Numbers*.

The *relative Turán number* for graphs  $G$  and  $F$ , denoted  $\text{ex}(G, F)$ , is the maximum number of edges in an  $F$ -free subgraph of  $G$ . In the special case  $G = K_n$ , we recover the well-researched Turán numbers  $\text{ex}(n, F)$ . In this talk we outline a proof for many graphs  $F$ , including all graphs of diameter at most three, of the conjecture of Foucaud, Krivelevich and Perarnau that every graph  $G$  of minimum degree  $d$  and maximum degree  $\Delta$  has a spanning  $F$ -free subgraph of minimum degree  $\Omega(d \cdot \frac{\text{ex}(\Delta, F)}{\Delta^2})$ . One of the ingredients is our proof that if  $G$  is a  $\Delta$ -regular graph, then  $G$  has a spanning subgraph of minimum degree at least  $\Delta/24$  which has a  $\Delta$ -coloring such that no two vertices at distance at most two have the same color. Our methods also show for many graphs  $F$  that  $\text{ex}(G, F) \geq d \cdot \frac{\text{ex}(\Delta, F)}{e\Delta^2}$ , which is tight up to a factor  $1/e$ . (Received August 30, 2016)