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Let us define, for a compact set  $A \subset \mathbb{R}^n$ , the Minkowski averages of  $A$ :

$$A(k) = \left\{ \frac{a_1 + \cdots + a_k}{k} : a_1, \dots, a_k \in A \right\} = \frac{1}{k} \left( \underbrace{A + \cdots + A}_{k \text{ times}} \right).$$

Shapley, Folkmann and Starr (1969) proved that  $A(k)$  converges to the convex hull of  $A$  in Hausdorff distance as  $k$  goes to  $\infty$ . Bobkov, Madiman and Wang (2011) conjectured that when one has convergence in the Shapley-Folkmann-Starr theorem in terms of a volume deficit, then this convergence is actually monotone. More precisely, they conjectured that  $|A(k)|$  is non-decreasing, where  $|\cdot|$  denotes Lebesgue measure.

In this talk, we show that this conjecture holds true in dimension 1 but fails in dimension  $n \geq 12$ . We also consider whether one can have monotonicity when measured using alternate measures of non-convexity, including the Hausdorff distance, effective standard deviation, and a non-convexity index of Schneider.

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