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Ross Geoghegan* (ross@math.binghamton.edu). *Parametrized Fixed Point Theory and Traces.*

I was lucky to work with Andy Nicas between 1986 and 2000 on 1-parameter fixed point theory; I'll discuss that work. In classical Nielsen theory a self-map $f : X \rightarrow X$ of a finite complex defines the Reidemeister trace - a souped-up Lefschetz number. It gives complete information about minimal number of fixed points of maps homotopic to f . For the certain kinds of maps this invariant can be interpreted as, roughly, the Hattori-Stallings trace (from K_0 to 0-dimensional Hochschild homology). In dimension 1, the map f is replaced by a homotopy $F : X \times I \rightarrow X$. We found a neat analog of the Reidemeister trace which gives significant information about the minimal possible number of "circles of fixed points" in homotopies homotopic to F . For certain kinds of homotopies our invariant can be interpreted as, roughly, the Dennis trace (from K_1 to 1-dimensional Hochschild homology). Among many results, this gave an elegant variation on the s-cobordism Theorem, saying that if the "trace of the Whitehead torsion" is non-zero then it is impossible to deform the top of the cobordism to the bottom without creating a circle of fixed points along the way. I'll describe this and some of our other theorems (quite widespread) having this general flavor. (Received July 21, 2017)