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**Eva Czabarka, Laszlo A. Szekely\*** (szekely@math.sc.edu) and **Stephan Wagner**. *Subtrees of trees*.

There is continuing interest in the distribution of small subgraphs of graphs by isomorphism type. For trees, to avoid a trivial answer, one has to investigate the distribution of subtrees of a given small size. We proved the following conjecture of Bubeck and Linial: if in a sequence of trees, where the tree size goes to infinity, the proportion of  $k$ -vertex paths among  $k$ -vertex subtrees becomes negligible, then almost all  $k$ -vertex subtrees are stars. We also showed that the maximum number of non-isomorphic subtrees (of all sizes) of trees on  $n$  vertices is  $\Theta(5^{n/4})$ .

Another way of looking for subtrees is the following: in a rooted binary tree, any  $k$  leaves induce a rooted subtree. To obtain the induced rooted binary subtree of this leaf set, suppress non-root vertices of degree 2. Now the natural question is the distribution of the  $k$ -leaf induced rooted binary subtrees. Results on this problem led to a proof that a randomly and uniformly selected  $n$ -leaf tanglegram has tanglegram crossing number  $\Theta(n^2)$  with near 1 probability. (Received August 18, 2016)