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**Martine Picavet\*** (picavet.gm@wanadoo.fr) and **Gabriel Picavet**. *FCP or FIP extensions and the Chinese Remainder Theorem.*

Let  $R \subseteq S$  be an extension of commutative rings and  $[R, S]$  the set of  $R$ -subalgebras of  $S$ . Then  $R \subseteq S$  is said to have FCP (resp. FIP) if each chain of the poset  $([R, S], \subseteq)$  is finite (resp.  $[R, S]$  is finite). The aim of this talk is to get an extension of the Chinese Remainder Theorem in the following sense. Let  $R$  be a ring,  $n > 1$  an integer and  $I_1, \dots, I_n$  ideals of  $R$  distinct from  $R$ , but not necessarily distinct, such that  $\bigcap_{j=1}^n I_j = 0$ . Consider the ring extension  $R \subseteq \prod_{j=1}^n (R/I_j) =: S$  with conductor  $C$ . This extension is an isomorphism if  $C = R$  (Chinese Remainder Theorem). We address the following questions: When is  $R \subseteq S$  a minimal extension, or more generally an FCP or FIP extension? We generalize a Ferrand-Olivier's result when  $n > 2$ . If  $R \subseteq S$  a minimal extension, then  $\{I_1, \dots, I_n\}$  satisfies a weak Chinese Remainder Theorem. We prove that  $R \subseteq S$  has FCP if and only if  $R/C$  is Artinian. If  $n = 2$ , we get that  $R \subseteq S$  has FIP if and only if  $R/(I_1 + I_2)$  has finitely many ideals. The characterization of the FIP property when  $n > 2$  is much more complicated. (Received September 10, 2016)