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Cohomology of picture groups for Dynkin quivers of type A. Preliminary report.

For every Dynkin quiver of finite representation type we define a finitely presented group called a picture group. This group is very closely related to the cluster theory of the quiver. For example, positive expressions for the Coxeter element in the group are in bijection with maximal green sequences. The picture group is derived from the semi-invariant picture for the quiver. We use this picture to construct a finite CW complex which has this group as its fundamental group i.e. is a K(π,1) for this group. The cells are in bijection with cluster tilting objects. For example, in type An there are a Catalan number of cells.

The main result is the computation of the cohomology ring of all picture groups of type $A_n$ with any orientation and any coefficient ring. (Received September 13, 2016)