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*Images of the countable ordinals.* Preliminary report.

In this paper, we study spaces that are continuous images of the usual space  $[0, \omega_1)$  of countable ordinals. We begin by showing that if  $Y$  is such a space and is  $T_3$  then  $Y$  has a monotonically normal compactification, is monotonically normal, locally compact, and scattered. Examples show that regularity is needed in these results. We investigate when a regular continuous image of the countable ordinals must be compact, paracompact, and metrizable. For example, we show that metrizability of such a  $Y$  is equivalent to each of the following:  $Y$  has a  $G_\delta$ -diagonal,  $Y$  is perfect,  $Y$  has a point-countable base,  $Y$  has countable cellularity,  $Y$  has a small diagonal in the sense of Hušek, and  $Y$  has a  $\sigma$ -minimal base. We give an example of a non-metrizable compact monotonically normal space every subspace of which is a paracompact p-space. We also obtain an absolute version of the Juhasz-Szentmiklossy theorem for small spaces by proving that if  $Y$  is any compact Hausdorff space having  $|Y| \leq \aleph_1$  and having a small diagonal, then  $Y$  is metrizable, and we deduce a recent result by Gruenhage on scattered compact spaces with small diagonals from work of Mrowka, Rajagopalan, and Soundararajan. (Received August 14, 2016)