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Lars Winther Christensen* (lars.w.christensen@ttu.edu), **Srikanth B Iyengar** and **Thomas Marley**. *Homological dimensions of modules over a commutative noetherian ring; what's new?*

For a finitely generated module M over a commutative noetherian local ring (R, \mathfrak{m}, k) , vanishing of $\mathrm{Tor}_{n+1}^R(k, M)$ for some $n \geq 0$ implies that M has finite flat dimension at most n . Similarly, vanishing of $\mathrm{Ext}_R^{n+1}(k, M)$ implies that M has finite injective dimension, as long as n is large enough, say, $n \geq \dim R$.

For modules that are not finitely generated, we prove similar statements that take all residue fields $k(\mathfrak{p}) = R_{\mathfrak{p}}/\mathfrak{p}R_{\mathfrak{p}}$ into account. (Received March 20, 2017)