

1129-20-237

**Daniela B Nikolova-Popova\*** (dpopova@fau.du), 777 Glades road, Boca Raton, FL 33435, and **Luise-Charlotte Kappe, Spyros Magliveras, Eric Swartz and Michael Epstein.** *On the Covering Number of Small Symmetric, Alternating Groups, and Some Sporadic Simple Groups.*

We say that a group  $G$  has a finite covering if  $G$  is a set theoretical union of finitely many proper subgroups. The minimal number of subgroups needed for such a covering is called the covering number of  $G$  denoted by  $\sigma(G)$ : Let  $S_n$  be the symmetric group on  $n$  letters. For odd  $n$  Maroti determined  $\sigma(S_n)$  with the exception of  $n = 9$ , and gave estimates for  $n$  even showing that  $\sigma(S_n) \leq 2n - 2$ . We show that  $\sigma(S_8) = 64$ ,  $\sigma(S_{10}) = 221$ ,  $\sigma(S_{12}) = 761$ . We also show that Maroti's result for odd  $n$  holds without exception proving that  $\sigma(S_9) = 256$ . We establish in addition that the Mathieu group  $M_{12}$  has covering number 208, and improve the estimate for the Janko group  $J_1$  given by P.E.Holmes. In another paper, we establish the covering number of  $A_9$ , and  $A_{11}$ . As of now, the smallest values of  $n$  for which the covering numbers of  $S_n$ , and  $A_n$  are not known are  $n=14$ , and  $n=12$  respectively. The methods we use involve GAP calculations, incidence matrices and linear programming. The coverings turn out to be dependent on the arithmetic nature of  $n$ . However, some results for larger classes of  $S_n$  have been established. (Received March 16, 2017)