

1129-60-202

**Moumanti Podder\*** (mp3460@nyu.edu), 226-230 East 12th Street, Apartment 11B, New York, NY 10012. *The Strange Logic of Galton-Watson Trees*.

This talk will focus on the rooted Galton-Watson (GW) tree with Poisson( $\lambda$ ) offspring distribution, though most of the results can be extended to very general distributions. I shall discuss first the analysis of first order (FO) properties: these capture the local structures inside a tree. I give a complete description of the probabilities  $P_\lambda[A]$  of all possible FO sentences  $A$  conditioned on the survival of the GW tree. There are, up to tautology, only a finite number of FO sentences of given quantifier depth  $k$ . For an arbitrary  $k$ , I introduce a natural distributional recursion  $\Psi_k$ , such that the probabilities of these sentences form a fixed point of  $\Psi_k$ . I further show that  $\Psi_k$  is a contraction, and that its fixed point is unique and analytic in  $\lambda$ .

Time permitting, I shall gloss over some recently finished results concerning existential monadic second order (EMSO) properties of trees. I define the notion of *interpretation* of fixed points derived from *tree automata*, and discuss a bit about *rogue fixed points*, the ones that do not admit any interpretation. I illustrate these via a nice example of an EMSO. I shall end with speculations and conjectures that hopefully the audience will find fascinating. (Received March 15, 2017)