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High-dimensional Nearest Neighbor Search (NNS) problem is a classic problem at the crossroads of theoretical computer science and machine learning. In one variant of it, we are given a high-dimensional pointset P , and we are to find the closest pair of points inside P , i.e., a pair at the smallest distance. The main objective is to obtain algorithms running faster than simply enumerating all pairs of points in P , perhaps at the expense of outputting only an approximately-closest pair. Past research has shown efficient approximate algorithms for standard distances such as the Euclidean or the ℓ_p norms.

We give an algorithm for the general problem of NNS under an *arbitrary high-dimensional symmetric norm*. The crux of the algorithm is a near-isometric embedding of an arbitrary symmetric norm into an universal norm, whose dimension is only polynomially-bounded in the dimension of the original symmetric norm. This universal norm is a product space of simpler norms, namely of ℓ_p 's and the top- k norm, for which we have (or design new) efficient algorithms. (Received March 19, 2017)