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*Axiomatizable classes of Banach spaces via disjointness preserving automorphisms.* Preliminary report.

Here  $\mathcal{C}$  is a class of Banach lattices and  $\mathcal{C}^{\mathcal{B}}$  is the class of underlying Banach spaces of members of  $\mathcal{C}$ . Both are considered as classes of metric structures, using continuous model theory with appropriate signatures. Recently Yves Raynaud published the following result [Thm 3.7, in *Positivity*, 2017]:

Theorem 1: Assume  $\mathcal{C}$  is axiomatizable, and every  $X \in \mathcal{C}$  satisfies: (a)  $X$  is order continuous; and (b) every linear isometric embedding from  $X$  into an ultrapower of  $X$  is disjointness preserving. Then  $\mathcal{C}^{\mathcal{B}}$  is axiomatizable.

Using model theory more explicitly (especially definability in continuous model theory), one can improve Theorem 1 by weakening assumption (b):

Theorem 2: Assume  $\mathcal{C}$  is axiomatizable, and every  $X \in \mathcal{C}$  satisfies: (a)  $X$  is order continuous; and (b) every surjective linear isometric map from  $X$  onto  $X$  is disjointness preserving. Then  $\mathcal{C}^{\mathcal{B}}$  is axiomatizable.

These theorems yield new examples and simpler proofs of known examples. (Received September 12, 2017)