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Florida Institute of Technology, 150 W. University Blvd, Melbourne, FL 32901. *Unique Solvability  
of Ill-posed Periodic Problem for a Higher Order Linear Hyperbolic Equation.*

**Abstract.** Consider the periodic problem

$$u^{(\mathbf{m})} = p(\mathbf{x})u + q(\mathbf{x}), \quad (1)$$

$$u(\mathbf{x} + \mathbf{T}_i) = u(\mathbf{x}) \quad (i = 1, \dots, n), \quad (2)$$

where  $n \geq 2$ ,  $\mathbf{x} = (x_1, \dots, x_n)$ ,  $\mathbf{T} = (T_1, \dots, T_n)$ ,  $\mathbf{T}_i = (0, \dots, T_i, \dots, 0)$ ,  $\mathbf{m} = (m_1, \dots, m_n)$ ,  $\|\mathbf{m}\| = m_1 + \dots + m_n$ . If  $\mathbf{l} = (l_1, \dots, l_n) \in \mathbb{Z}_+^n$ , then by  $C_{\mathbf{T}}^{\mathbf{l}}(\mathbb{R}^n)$  denote the space of continuous functions  $u : \mathbb{R}^n \rightarrow \mathbb{R}$  satisfying (2) and having continuous partial derivatives  $u^{(\mathbf{k})}$ , ( $\mathbf{k} \leq \mathbf{l}$ ).

**Theorem.** Let  $\mathbf{m} = 2\mathbf{m}^*$ ,

$$(-1)^{\|\mathbf{m}^*\|} p(\mathbf{x}) \leq 0,$$

$$(-1)^{\|\mathbf{m}^*\|} \int_0^{T_j} p(x_1, \dots, s_j, \dots, x_n) ds_j < 0 \quad (j = 1, \dots, n),$$

and let  $p, q \in C_{\mathbf{T}}^{\mathbf{l}}(\mathbb{R}^n)$ . Then problem (1), (2) has a unique (weak, if  $\mathbf{l} \prec \mathbf{m}$ ) solution  $u \in C_{\mathbf{T}}^{\mathbf{l}}(\mathbb{R}^n)$ . (Received July 31, 2017)