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Under the condition that the weight function W is positive and continuous on $[0, \infty)$ and satisfies $\frac{-\ln W(x)}{x^\alpha} \rightarrow \infty$ as $x \rightarrow \infty$ for some $\alpha > 1$, then the approximation theorem of Weierstrass is shown to hold for $f(x) \in C_W^0[0, \infty)$, the set of continuous functions for which $W(x)f(x) \rightarrow 0$ as $x \rightarrow \infty$.

Similarly, if W defined on $(-\infty, \infty)$ and is positive and continuous and satisfies $\frac{-\ln W(x)}{x^{2\alpha}} \rightarrow \infty$ as $x \rightarrow \pm\infty$ for some $\alpha > 1$, then the approximation theorem of Weierstrass is shown to hold for $f(x) \in C_W^0(-\infty, \infty)$, the set of continuous functions for which $W(x)f(x) \rightarrow 0$ as $x \rightarrow \pm\infty$.

The proofs of the above two results will be based upon a generalization by Chlodowsky of the Bernstein polynomial operators.

These results are presented in memory of Katalin Balázs 08/13/1949 - 09/07/2016, who was for 26 years my mathematical collaborator and my very devoted and very beloved wife. (Received July 27, 2017)