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**John E. Herr\*** (jeherr@butler.edu), **Palle E.T. Jorgensen** (palle-jorgensen@uiowa.edu) and **Eric S. Weber** (esweber@iastate.edu). *Constructions and a Characterization of Positive Matrices in the Hardy Space with Prescribed Boundary Representations.*

Using the Kaczmarz algorithm, for any singular Borel probability measure  $\mu$  on the unit circle, we use a Parseval frame in  $L^2(\mu)$  “dextrodual” to the sequence  $\{e^{2\pi inx}\}_{n=0}^{\infty}$  to construct positive matrices in  $H^2(\mathbb{D})$  that have  $L^2(\mu)$  boundary function representations and are reproducing kernels with respect to those representations. For a given positive matrix  $K$  in  $H^2(\mathbb{D})$  of a common form and a Borel measure  $\mu$  on the unit circle, we give a characterization of when  $K$  has  $L^2(\mu)$  boundary representations. This characterization is in terms of a matrix identity based on a new operator product called the Abel product. (Received February 01, 2018)