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All sub-semirings of the field  $\mathbb{Q}$  that are not rings (i.e., rational semirings) are contained in the nonnegative cone of  $\mathbb{Q}$ . It has been proved that the rational semiring  $S_r$  generated by a given positive rational  $r$  (i.e., the cyclic rational semiring generated by  $r$ ) is atomic as an additive monoid unless  $r = 1/n$  for some  $n \in \mathbb{N}$ . Thus, “almost all” cyclic rational semirings are atomic monoids. Here we study some of the most relevant factorization invariants of the cyclic rational semirings. Since  $S_r$  is nicely generated as a monoid, that is  $S_r := \langle r^n \mid n \in \mathbb{N}_0 \rangle$ , we are able to give a detailed description of many of its factorization invariants. A very distinguished factorization property of any atomic cyclic rational semiring  $S_r$  is that all its sets of lengths are arithmetic sequences with a common distance. We prove this result, and then use it to discuss further factorization invariants including the elasticity, omega primality, and tameness of  $S_r$ . (Received January 28, 2019)