Iwasawa theory concerns how certain arithmetic data varies in p-adic families. Modular (and, more generally, automorphic) forms have turned out to play a key role in studying this data. In this talk, I will introduce some tools (in particular, differential operators) for studying p-adic aspects of automorphic forms, as well as arithmetic consequences. (Received January 10, 2019)