I will talk about my joint work with David Jarossay. I will explain that the special values at tuples of positive integers of the $p$-adic multiple $L$-function, introduced by Furusho, Komori, Matsumoto and Tsumura, can be expressed in terms of the cyclotomic multiple harmonic values introduced by Jarossay. (Received January 25, 2019)